CHAPTER 3 MATLAB EXERCISES



(a)
$$\begin{bmatrix} 2 & -3 \\ -6 & 9 \end{bmatrix}$$
 (b) $\begin{bmatrix} -5 & 6 & 7 \\ 0 & -1 & 2 \\ 4 & 0 & -3 \end{bmatrix}$

(c) pascal(4)

(d) hilb(8)

2. Let

$$A = \begin{bmatrix} 1 & 4 \\ 2 & -1 \end{bmatrix}.$$

Use the MATLAB determinant command **det** to compute $\det(2 * \exp(2) - A)$. Find an integer value of t such that $\det(tI - A) = 0$.

- **3.** Choose arbitrary 4×4 matrices A and B. Compute $\det(A) \det(B)$, and $\det(AB)$. What do you observe? Do the same for $\det(A) + \det(B)$ and $\det(A + B)$.
- **4.** Choose an arbitrary real number t. Form the matrix

$$A = \begin{bmatrix} \cos(t) & \sin(t) \\ -\sin(t) & \cos(t) \end{bmatrix}$$

and calculate its determinant. Does the value of the determinant depend on t?

5. Consider the matrices

$$A = \begin{bmatrix} 2 & 0 & 1 \\ 1 & -1 & 2 \\ 3 & 1 & 1 \end{bmatrix} \quad \text{and} \quad B = \begin{bmatrix} 2 & -1 & 4 \\ 0 & -1 & 3 \\ 3 & -2 & 1 \end{bmatrix}.$$

- (a) Verify that det(A) det(B) = det(AB).
- (b) Verify that $det(A^T) = det(A)$.
- (c) Verify that $det(A^{-1}) = 1/det(A)$.
- **6.** In this exercise, we will use Cramer's Rule to solve the linear system $A\mathbf{x} = \mathbf{b}$ from Example 3, Section 3.4. Let

$$A = \begin{bmatrix} 4 & -2 \\ 3 & -5 \end{bmatrix} \quad \text{and} \quad \mathbf{b} = \begin{bmatrix} 10 \\ 11 \end{bmatrix}$$

be the coefficient matrix and the right-hand side, respectively. To form the matrix A_1 , we need to replace the first column of A with \mathbf{b} . To do this, type

$$A1 = A$$

$$A1(:,[1]) = b$$

The solution x_1 is obtained by typing

det(A1)/det(A)

You can calculate x_2 in a similar manner.

$$A2 = A$$

 $A2(:,[2]) = b$
 $det(A2)/det(A)$

7. Use the Cramer's Rule algorithm from Exercise 6 to solve the following linear system. Compare your answer with that obtained using **rref**.

$$3x + 3y + 4z = 2$$

$$x + y + 4z = -2$$

$$2x + 5y + 4z = 3$$